

experiences understanding what the mean reflects about the data and how changes in data will affect the average. The purpose of statistics is to give a picture about the data. Students need to be able to use other measures of center, like median and range, to help them make sense of the situation.

**6<sup>th</sup> grade**

**Task 2**

**Gym**

<b>Student Task</b>	Analyze gym membership costs to solve a practical money problem.
<b>Core Idea 3 Algebra and Functions</b>	<p><b>Understand relations and functions, analyze mathematical situations, and use models to solve problems involving quantity and change.</b></p> <ul style="list-style-type: none"> <li>• Model and solve contextualized problems using various equations</li> </ul>
<b>Core Idea 1 Number and Operation</b>	<p><b>Understand number systems, the meanings of operations, and ways of representing numbers, relationships, and number systems</b></p> <ul style="list-style-type: none"> <li>• Understand and use proportional reasoning to represent quantitative relationships</li> </ul>

---

## Gym

This problem gives you the chance to:

- select relevant data and operations
  - solve a practical money problem
- 

Carlo wants to join a gym.

The gym offers three membership options.

<b>Pay as you go</b> Pay only \$6 each time you work out	<b>Regular deal</b> Pay \$50 a month and \$2 each time you work out
<b>All-in-one price!</b> Pay just \$100 per month for unlimited use of our great facilities	

1. Carlo thinks he will go to the gym about 20 times a month.  
Calculate how much each of these options would cost Carlo for one month.

Pay as you go \$ \_\_\_\_\_

Regular deal \$ \_\_\_\_\_

All-in-one price \$ \_\_\_\_\_

Which of these options is the least expensive for Carlo? \_\_\_\_\_

2. How many visits each month would make the cost of the **Regular deal** and the **All-in-one price** the same?

\_\_\_\_\_

Explain how you figured it out.

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

3. It costs \$300 to join the new Superfit Gym. You then pay \$15 each month and \$2 each time you work out. Carlo thinks he will use the gym about 20 times each month for a year.

Calculate the cost of using the Superfit Gym for one year.

\_\_\_\_\_

How much will Carlo save during the first year if he uses the Superfit Gym rather than the Regular deal at the other gym?

\_\_\_\_\_

Show your work.

<b>Gym</b>		<b>Test 6 Form A Rubric</b>	
<p>The core elements of performance required by this task are:</p> <ul style="list-style-type: none"> <li>• select relevant data and operations</li> <li>• solve a practical money problem</li> </ul> <p>Based on these, credit for specific aspects of performance should be assigned as follows:</p>		<b>Points</b>	<b>Section Points</b>
<p>1. Gives correct answer as:</p> <p>Pay-as-you-go price for 20 visits = <b>\$120</b></p> <p>Regular deal price for 20 visits = <b>\$90</b></p> <p>All-in-one price is <b>\$100</b></p> <p><b>Regular deal</b></p> <p>Four correct answers: 3 points</p> <p><i>Partial credit:</i></p> <p>Three correct answers: 2 points</p> <p>Two correct answers: 1 point</p>		3  (2) (1)	3
<p>2. Gives correct answer as:</p> <p><b>25 visits</b></p> <p>Shows calculations such as:</p> <p><math>100 - 50 = 50</math></p> <p><math>50 \div 2 = 25</math></p>		1   1	2
<p>3. Gives correct answer as:</p> <p><b>\$960.00</b></p> <p>Gives correct answer as:</p> <p><b>\$120</b></p> <p>Shows calculations such as:</p> <p>Superfit: <math>300 + 180 + 480 = 960</math></p> <p>Regular: <math>600 + 480 = 1,080</math></p>		1  1  1	3
<b>Total Points</b>			<b>8</b>

## Looking at Student Work – Gym

Students seem to have a difficult time analyzing the effects of operations on units (dimensional analysis) and making comparisons. Student A does a good job of tracking the units as he works through different parts of the task. The work is organized in a manner that makes the logic very easy to follow. Part 3 starts with the cost of visits per month to visits per year, then monthly fee to yearly fee, and finally total cost.

### Student A

<b>Pay as you go</b> Pay only \$6 each time you work out	<b>Regular deal</b> Pay \$50 a month and \$2 each time you work out
<b>All-in-one price!</b> Pay just \$100 per month for unlimited use of our great facilities	

1. Carlo thinks he will go to the gym about 20 times a month.  
 Calculate how much each of these options would cost Carlo for one month.

Pay as you go

\$ 120.00 ✓

Regular deal

\$ 90.00 ✓

All-in-one price

\$ 100.00 ✓

Which of these options is the least expensive for Carlo?

Regular deal ✓

Pay as you go	Regular deal	All-in-one price
$20 \text{ times} \\ \times \$6 \text{ dollars} \\ \hline \$120 \text{ dollars}$	$\begin{array}{r} 20 \text{ times} \\ \times 2 \text{ dollars} \\ \hline 40 \\ 50 \text{ dollars} \\ + 40 \text{ dollars} \\ \hline 90 \text{ dollars} \end{array}$	$100.00 \text{ dollars}$

Student A

2. How many visits each month would make the cost of the Regular deal and the All-in-one price the same?

$100 = \text{All-in-one price}$   
 $90 = \text{Regular deal}$   
 $10$   
 $\frac{10}{2} = 5$   
 $20 + 5 = 25$  visits ✓

Explain how you figured it out.

First of all, I subtracted \$90 from \$100 to see the difference (which was \$10). Since you pay \$2 a visit I divided \$10 by \$2 (which was 5). I then added five to the 20 visits to make it 25 visits for \$100.00.

3. It costs \$300 to join the new Superfit Gym. You then pay \$15 each month and \$2 each time you work out. Carlo thinks he will use the gym about 20 times each month for a year.

Calculate the cost of using the Superfit Gym for one year.

\$960.00 ✓

How much will Carlo save during the first year if he uses the Superfit Gym rather than the Regular deal at the other gym?

\$120.00 ✓

Show your work.

The cost	save
$\begin{array}{r} 300 \\ + 180 \\ \hline 480 \\ + 480 \\ \hline 960 \end{array}$	$\begin{array}{r} 300.00 = \text{reg deal} \\ 960.00 = \text{superfit} \\ \hline 120.00 \end{array}$
$\begin{array}{r} 20 \\ \times 2 \\ \hline 40 \end{array}$	$\begin{array}{r} 90 \text{ dollars} \\ \times 12 \text{ visits} \\ \hline 3 \end{array}$
$\begin{array}{r} 40 \text{ dollars} \\ \times 12 \text{ months} \\ \hline 480 \end{array}$	
$\begin{array}{r} 15 \text{ dollars} \\ \times 12 \text{ visits} \\ \hline 180 \end{array}$	

Student B makes the most common error in part 3. The student finds the yearly cost of gym visits and yearly total for monthly fees, but forgets to add in the cost of joining the gym.

### Student B

2. How many visits each month would make the cost of the Regular deal and the All-in-one price the same?

Explain how you figured it out.

I solved it by  $100 - 50$  and I got  $50 \div 2$  and got 25 visits

$$\begin{array}{r} \$100 \\ - \$50 \\ \hline 50 \end{array} \quad \begin{array}{r} 25 \\ \times 2 \\ \hline 50 \\ + 50 \\ \hline 100 \end{array} \quad \begin{array}{r} 25 \text{ visits} \\ \times 2 \\ \hline 50 \\ + 50 \\ \hline 100 \end{array} \quad \begin{array}{r} 25 \text{ visits} \\ \times 2 \\ \hline 50 \\ + 50 \\ \hline 100 \end{array}$$

3. It costs \$300 to join the new Superfit Gym. You then pay \$15 each month and \$2 each time you work out. Carlo thinks he will use the gym about 20 times each month for a year.

Calculate the cost of using the Superfit Gym for one year.

How much will Carlo save during the first year if he uses the Superfit Gym rather than the Regular deal at the other gym?

Show your work:

$$\begin{array}{r} 20 \\ \times 2 \\ \hline 40 \\ + 50 \\ \hline 90 \\ \times 12 \\ \hline 180 \\ 900 \\ \hline \$1080 \\ - 660 \\ \hline \$420 \end{array} \quad \begin{array}{r} 20 \\ \times 2 \\ \hline 40 \\ \times 12 \\ \hline 480 \\ + 300 \\ \hline 780 \end{array} \quad \begin{array}{r} 480 \\ + 180 \\ \hline 660 \end{array} \quad \begin{array}{r} 15 \\ \times 12 \\ \hline 30 \\ \times 12 \\ \hline 180 \end{array} \quad \begin{array}{r} 660 \\ + 180 \\ \hline 840 \end{array}$$

Student C finds the cost per month of visits and fees and compares them to the cost per month of the Regular deal gym. This would have worked if the student had additionally found the monthly cost of the initiation fee (\$25) and added that to the Superfit total. The student would still have needed to multiply the difference by 12 to find the yearly difference.

### Student C

3. It costs \$300 to join the new Superfit Gym. You then pay \$15 each month and \$2 each time you work out. Carlo thinks he will use the gym about 20 times each month for a year.

Calculate the cost of using the Superfit Gym for one year.

$$\frac{\$55}{\cancel{\times 0}}$$

How much will Carlo save during the first year if he uses the Superfit Gym rather than the Regular deal at the other gym?

$$\frac{\$35}{\cancel{\times 0}}$$

Show your work

$$\begin{array}{r} 20 \\ \times 2 \\ \hline 40 \\ +15 \\ \hline 55 \end{array}$$

$$\frac{\cancel{40}}{\times 0}$$

(3)

Student D makes two common errors. In part 2 of the task the student confuses the increase in number of visits with the total number of visits. In part 2 the student finds the cost of 20 visits per month, but forgets to multiply that number by 12 to find the cost for visits per year.

**Student D**

How many visits each month would make the cost of the **Regular deal** and the **one price** the same?

$$\frac{5}{1} \checkmark$$

Explain how you figured it out.

$$\begin{array}{r} 20 \\ \times 5 \\ \hline 100 \end{array} \quad 2 \times 5 = 10$$

It costs \$300 to join the new Superfit Gym. You then pay \$15 each month and \$2 each time you work out. Carlo thinks he will use the gym about 20 times each month for one year.

Calculate the cost of using the Superfit Gym for one year.

$$520 \times 1$$

How much will Carlo save during the first year if he uses the Superfit Gym rather than the regular deal at the other gym?

$$560 \times$$

Show your work.

$$\begin{array}{r} 300 \\ + 180 \\ + 40 \\ \hline 520 \end{array} \quad \begin{array}{r} 15 \\ \times 12 \\ \hline 180 \end{array} \quad \begin{array}{r} 20 \\ \times 9 \\ \hline 180 \end{array} \quad \begin{array}{r} 300 \\ + 180 \\ + 90 \\ \hline 570 \\ - 10 \\ \hline 560 \times \end{array}$$

Student E forgets the monthly cost for regular deal and finds the number of visits that will equal all-in-one price. Students have difficulty keeping track of the different constraints or features involved in the different pricing schemes.

### Student E

2. How many visits each month would make the cost of the **Regular deal** and the **All-in-one price** the same?

$$\frac{50}{x} \times$$

Explain how you figured it out.

The all-in-one is \$100 every month the Regular deal is \$2 every time you work out. 50 day  $\times$  the \$2 price of Regular deal would be \$100, which means  $50 \times 2 = 100$  All-in is \$100

### Teacher Notes:

---

---

---

---

---

---

---

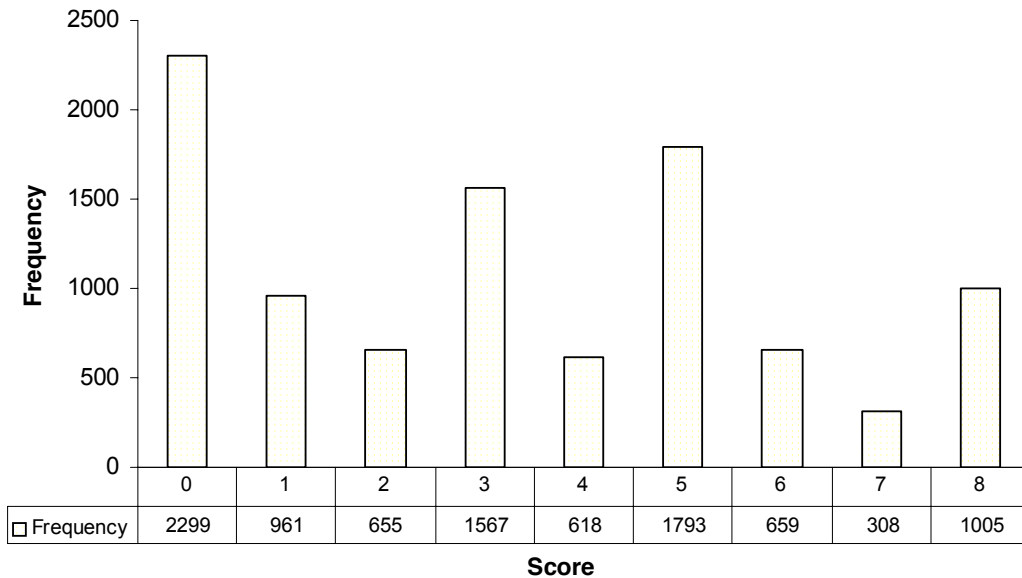
---

---

Grade 6 – Gym

**Gym**

Mean: 3.30, S.D.: 2.63



Score:	0	1	2	3	4	5	6	7	8
% < =	23.3%	33.0%	39.7%	55.6%	61.8%	80.0%	86.7%	89.8%	100.0%
% > =	100.0%	76.7%	67.0%	60.3%	44.4%	38.2%	20.0%	13.3%	10.2%

The maximum score available for this task is 8 points.  
The cut score for a level 3 response is 3 points.

Most students (about 80%) could find the cost of the Pay as you go plan and the All-in-one plan. A little more than half of the students (about 67%) could correctly calculate the costs of all three options and compare to find the better deal. Almost 44% could compare the 3 options and find the number of visits that would make All-in-one and regular deal the same. About 10% of the students could meet all the demands of the task, including comparing the yearly costs and savings of two different gym plans. Almost 20% of the students scored no points on this task. 90% of those students attempted the task.

## Gym

Points	Understandings	Misunderstandings
<b>0</b>	Almost 20% of the students scored no points on this task. 90% of the students with this score attempted the problem.	Students had difficulty calculating the costs for Regular deal. Many students put \$50 (just the monthly fee), \$100 (50 x 2), \$52 (50+2), 1000 (20 x 50), or 2000 (40x 50) . These answers make up 19% of the responses. They could not reason clearly about how the how visits, costs per visit, and monthly costs fit together. They are testing out operations without thinking through how those operations contribute to the solution.
<b>1</b>	Students with this score could generally find the monthly cost for Pay as you go and All-In-One deal.	
<b>3</b>	Students could find the monthly cost of all the gym plans and compare to find the best value.	Students had trouble finding the number of visits to equalize the cost for regular plan and All-In-One. About 10% of all the students did not attempt this part of the task. Another 10% thought there would need to be 50 visits, forgetting to include the monthly fee in their calculations. About 12% thought the number of monthly visits would be 2 or 5.
<b>5</b>	Students could find the monthly costs of all the gym plans and find the number of visits needed at the Regular Price to equal the cost of the All-in-one plan.	Students had difficulty dealing with all the constraints for comparing the yearly costs of Superfit and Regular Deal. Almost 10% of the students forgot to add in the initiation fee for Superfit. Another 10% forgot to multiply the cost of monthly visits by 12, so they got a total cost of \$520 instead of \$960.
<b>6</b>		Students with this score could not find the number of visits needed in part two of the task or could not complete the comparison in part 3 even though they correctly found the yearly cost for Superfit.
<b>8</b>	Students could calculate and compare different options for gym memberships in dollars and number of visits.	

*Based on teacher observations, this is what sixth grade students seemed to know and be able to do:*

- Calculate the costs of different options for gym memberships for one month
- Compare costs of the different options
- Find the number of visits needed in one plan to equal the cost with another plan

*Areas of difficulty for sixth graders, sixth grade students struggled with:*

- Identifying and using multiple constraints within the different gym options
- Analyzing the affects of operations on units (e.g. adding visits to dollars)
- Converting all constraints to the same measure to allow a comparison (e.g. forgetting to converting cost of visits per month to cost of visits per year)

### **Questions for Reflection on Gym:**

- Look at the errors in student work for finding the monthly cost of regular deal. What types of error patterns do you see? What were students thinking about and not thinking about? Were the errors caused by ignoring constraints? Not understanding the units?
- How did your students make sense of part 2? How many put:

50	5	2	8	95	4000

What is the logic behind each wrong answer? Is the logic consistent for each wrong answer? What are the implications for further instruction?

- Look at the work for students in part 3. How many of your students put:

660	600	520	300	180	240

- What is the logic behind each wrong answer? Is the logic errors related to the types of errors you noticed in part 2 or different? In what way? How would you summarize student thinking?
- What are the implications for further instruction? Do students need more work with units? With the logic of comparisons? Problems dealing with multiple constraints? Models to help them understand the effects of operations on numbers? Organizational tools? What is your evidence?

### **Teacher Notes:**

---



---



---



---

**Instructional Implications:**

Students need more experiences making comparisons. They need to calculate the full costs of both options before making a decision. It is not enough to just calculate the cost for the favored choice. Students might consider different choices about family entertainment options or cell phone plans to determine the best price. Students lack experience analyzing the effects of operations on units or systems for keeping track of units as they work through steps in a problem. Dimensional analysis is a topic that many teachers need to deal with more explicitly. Students also have trouble identifying the various constraints of within each option and seeing how they interconnect. Students need to work with more problems in context instead of working isolated number calculation skill sets.